## 4725 Further Pure Mathematics 1

1 (i) $\left(\begin{array}{cc}a-4 & 2 \\ 3 & 0\end{array}\right)$ B1 Two elements correct

B1 2 Remaining elements correct

| (ii) $4 a-6$ | B1 | Correct determinant |
| :--- | :--- | :--- |
|  | M1 | Equate det A to 0 and solve |
|  | $a=\frac{3}{2}$ | A1 |
|  | 3 | Obtain correct answer a. e. f. |

2 (i) \begin{tabular}{lll}

$u^{3}-3 u^{2}+3 u-1$ \& B1 \& | Correct unsimplified expansion of |
| :--- |
| $(u-1)^{3}$ | <br>

\& M1 \& Substitute for $x$ <br>
$2 u^{3}-6 u^{2}+9 u-8=0$ \& A1 \& 3

 

Obtain correct equation
\end{tabular}

(ii)

4
M1 Use $( \pm) \frac{d}{a}$ of new equation
A1ft 2 Obtain correct answer from their equation

## 5

| 3 | $x-\mathrm{i} y$ |  | B1 |  | Conjugate known |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | M1 |  | Equate real and imaginary parts |
|  | $x+2 y=12$ | $2 x+y=9$ | A1 |  | Obtain both equations, OK with factor of i |
|  |  |  | M1 |  | Solve pair of equations |
|  | $z=2+5 i$ |  | A1 | 5 | Obtain correct answer as a complex number |
|  |  |  |  |  | S.C. Solving $z+2 \mathrm{iz}=12+9 \mathrm{i}$ can get $\max \quad 4 / 5$, not first B1 |
|  |  |  | 5 |  |  |

4
M1
Express as sum of three series
M1
A1
M1 Attempt to factorise
A1
Obtain at least factor of $n(n+1)$
A1 6 Obtain fully factorised correct answer

| (i) | B1 | Rotation $90^{\circ}$ (about origin) |
| :--- | :--- | :--- | :--- |
| (ii) Either | B1 | Anticlockwise |


(ii) $\frac{1}{\Delta}\left(\begin{array}{c}5 a-7 \\ 4 a-5 \\ 3\end{array}\right)$

M1 Attempt product of form $\mathrm{A}^{-1} \mathrm{C}$ or eliminate to get 2 equations and solve

A1A1A1 Obtain correct answer ft all 3

4 S.C. if det now omitted, allow max A2 ft 11

10 (i)

$$
\mathbf{M}^{2}=\left(\begin{array}{ll}
1 & 4 \\
0 & 1
\end{array}\right) \quad \mathbf{M}^{3}=\left(\begin{array}{ll}
1 & 6 \\
0 & 1
\end{array}\right)
$$

B1 Correct $\mathbf{M}^{2}$ seen
M1 Convincing attempt at matrix multiplication for $\mathbf{M}^{3}$
A1 3 Obtain correct answer
(ii) $\mathbf{M}^{n}=\left(\begin{array}{cc}1 & 2 n \\ 0 & 1\end{array}\right)$

B1ft 1 State correct form, consistent with (i)

| 10 (iii) | $\begin{aligned} & \text { M1 } \\ & \text { A1 } \\ & \text { A1 } \\ & \text { B1 } \end{aligned}$ | Correct attempt to multiply $\mathbf{M} \& \mathbf{M}^{k}$ or v.v. <br> Obtain element $2(k+1)$ <br> Clear statement of induction step, from correct working <br> Clear statement of induction conclusion, following their working |
| :---: | :---: | :---: |
| (iv) | B1 <br> DB1 <br> DB1 3 <br> 11 | Shear <br> $x$-axis invariant e.g. $(1,1) \rightarrow(21,1)$ or equivalent using scale factor or angles |

